

Introduction to Bond Markets

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- A bond is a financial security that promises to pay a fixed (known) income stream in the future
- Issued by governments, state agencies (municipal bonds), and corporations
- Bonds are characterized by
 - Maturity date
 - Face, par or principal value (i.e., the notional amount typically 1000)
 - Coupon rate
 - number of coupon payments/ year (typically 2)

Repayment types

- Pure discount or zero coupon bonds: Bonds that pay no interest (coupon). They sell at a discount (price below par) to provide investor with positive return.
- Coupon bonds. Pays fixed coupon at known times. For example, A November 2021 maturity, 8% government bond will pay its owner $40 = 8\% * 1000/2$ every April 15th and November 15th in addition to 1000 at expiration on November 15th, 2021.
- Floating rate. Pays variable rate coupons linked to some benchmark rate. Example: Inflation indexed bonds' (I-bonds) coupon rate is determined by the level of inflation (as measured by the relative change in the CPI)

US government bonds are interesting because

- The default risk is thought of as zero (although it may not be)
- They are highly liquid
- They provide a basic benchmark for other fixed income securities including other sovereign bonds, corporates, munis, etc.

\$50

The United States of America

FOR VALUE RECEIVED PROMISES TO PAY TO

\$50


 DEFENSE SAVINGS BOND
 SERIES E
 ISSUED BY THE U.S. GOVERNMENT
 FIRST DAY OF

SPECIMEN

 DUE 10 YEARS
 FROM SUCH DATE

L2E

FIFTY DOLLARS

WITHOUT INTEREST, TEN YEARS FROM THE DATE AS OF WHICH THIS BOND IS ISSUED. THIS BOND IS redeemable AT THE OPTION OF THE OWNER DURING ANY PERIOD AFTER SAID ISSUE DATE (BUT NOT WITHIN THE FIRST SIXTY DAYS) IN AN AMOUNT EQUAL TO ITS REDEMPTION VALUE DURING THAT PERIOD AS SHOWN BY THE FOLLOWING

TABLE OF REDEMPTION VALUES

DURING SUCCESSIVE PERIODS AFTER ISSUE DATE

ISSUE PRICE—\$57.50

FIRST 6 MONTHS.....	\$57.50	2 1/2 TO 3 YEARS.....	\$58.50	3 TO 3 1/2 YEARS.....	\$41.00	7 1/2 TO 8 YEARS.....	\$45.00
6 TO 1 YEAR.....	\$57.50	3 TO 3 1/2 YEARS.....	\$58.50	3 1/2 TO 4 YEARS.....	\$41.50	8 TO 8 1/2 YEARS.....	\$45.25
1 TO 1 1/2 YEARS.....	\$57.50	3 1/2 TO 4 YEARS.....	\$59.00	4 TO 4 1/2 YEARS.....	\$42.00	8 1/2 TO 9 YEARS.....	\$45.50
1 1/2 TO 2 YEARS.....	\$58.00	4 TO 4 1/2 YEARS.....	\$59.50	4 1/2 TO 5 YEARS.....	\$42.50	9 TO 9 1/2 YEARS.....	\$46.00
2 TO 2 1/2 YEARS.....	\$58.50	4 1/2 TO 5 YEARS.....	\$60.00	5 TO 5 1/2 YEARS.....	\$43.00	9 1/2 TO 10 YEARS.....	\$46.50

NATURALITY VALUE 10 YEARS FROM ISSUE DATE—\$50.00

THIS IS A DEFENSE SAVINGS BOND OF SERIES E, OF AN ISSUE OF UNITED STATES SAVINGS BONDS AUTHORIZED BY THE SECOND LIBERTY BOND ACT, AS AMENDED, AND ISSUED PURSUANT TO TREASURY DEPARTMENT CIRCULAR NO. 889, DATED APRIL 15, 1941, TO WHICH REFERENCE IS MADE FOR A STATEMENT OF THE RIGHTS OF HOLDERS AS FULLY AND WITH THE SAME EFFECT AS THOUGH HEREIN SET FORTH.

THIS BOND IS NOT TRANSFERABLE, FOR A CASH OR PROCEEDS UNDER SAID CIRCULAR, UNTIL PAYABLE AT MATURITY OR IN EARLIER PERIODS, ONLY TO THE REGISTERED OWNER AND ONLY TO THE PERSONS OR PERSONS NAMED IN THE PROVISIONS OF SAID CIRCULAR AND THE REGULATIONS PRESCRIBED THEREIN FROM TIME TO TIME.

THIS BOND SHALL BE VALID ONLY IF ENDORSED WITH THE OWNER'S NAME AND SIGNATURE AT THE FIRST DAY OF THE MONTH IN WHICH THE ISSUE PRICE IS RECEIVED, AND ONLY EMPLOYED BY AN OWNER AS PART OF HIS INCOME TAX PAYMENTS. THE AMOUNT OF DEFENSE SAVINGS BONDS REGISTERED IN HIS NAME SHALL NOT BE MORE THAN THE AMOUNT OF DEFENSE SAVINGS BONDS REGISTERED IN HIS NAME UNDER ANY OTHER NAME OR UNDER ANY OTHER PERSON. THE BOND AT ANY ONE TIME SHALL NOT EXCEED \$5,000 IN MATURITY VALUE.

TREASURY DEPARTMENT, WASHINGTON

NOT TRANSFERABLE

DEFENSE SAVINGS BOND

 Henry Morganstein Jr.
 1941-1951 Treasury

\$50

DEFENSE SAVINGS BOND

\$50

WHO IN WASHINGTON
IS RESPONSIBLE FOR

THE

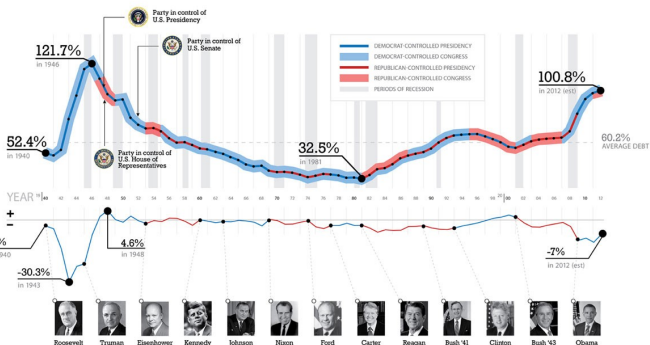
U.S. DEBT

???

With all the talk lately about the debt ceiling, we wanted to take a look at how we got here. While political parties play the blame game, the facts paint a more complicated picture. The data shows that both parties have presided over huge increases and decreases in our national debt, and that events like World War 2 and periods of recession have often been far more important than party ideology.

UNITED STATES DEBT AS A PERCENTAGE OF GDP (1940 - 2012 EST)

Measuring U.S. debt in numbers that haven't been adjusted for inflation produces an alarming and somewhat misleading result. $\frac{163}{100} = 1.63$ times of value.
Measuring U.S. debt as a percentage of GDP gives us a much better idea of who our biggest borrowers have been.



BUDGET SURPLUSES & DEFICITS AS A PERCENTAGE OF GDP

Some presidents are better at balancing budgets than others. Despite labels such as fiscal conservative or big government liberal, the data shows that the ability or inability to balance budgets is truly bi-partisan.

HOW THE RATIO OF US DEBT COMPARES TO OTHER COUNTRIES.

The range is enormous due to emerging third world markets and wild swings created by the economic collapse. (Public Debt/GDP)



elefintdesigns.com | Sources: CIA World Fact Book, White House Office of Management and Budget.

Designed by **elefint designs**

Government bonds come in three varieties:

- Bills. These are zero coupon bonds with maturities less than one year
- Notes. Semi-annual coupon bonds with maturities less than 10 years
- Bonds. Semi-annuals with more than 10 year maturity

- Govt bonds are sold in the primary market through auctions.
- Bids submitted through dealers or directly to the treasury
- Competitive and non-competitive bids:
 - competitive bid: bidder submits amount and price (as in limit order)
 - non-competitive: quantity demanded at clearing price (as in market order)
- Market clearing: Non-competitive bids subtracted from total supply. Market clears by matching supply with demand from competitive bids. Single price auction mechanism means that the marginal bid determines the auction price.

Secondary Markets

- No standardized exchange as with stocks
- Sold over-the-counter through dealers or the treasury themselves (treasurydirect.gov)
- Dealer quotes displayed through Bloomberg. BGCantor live data available from them
- $t + 1$ settle: trades are settled the day after executed.

Treasury Bills are zero coupon bonds issued with less than one year maturity.

T-Bills are quoted at a *discount basis*. Let d denote the discount basis, then the price you pay, P , is

$$P = 100\left(1 - d\frac{t}{360}\right) \quad (1)$$

where t is the number of calendar days to expiration.

<HELP> for explanation.

United States

1) Actions

2) Tools

3) Settings

Fixed Income Trading

13:03

4) Actives

5) Bills

6) Notes

7) TIPS

8) Strips

9) Sprds

10) Curves

11) FRN

12) Bfly

13) WI

		BidPx / AskPx	AskYld	YChg			BidPx / AskPx	AskYld	YChg
31)	12/11/14	0.045 / 0.040	0.041	--	50)	03/26/15	0.025 / 0.020	0.020	--
32)	12/18/14	0.045 / 0.040	0.041	-0.010	51)	04/02/15	0.040 / 0.035	0.035	--
33)	12/26/14	0.075 / 0.070	0.071	-0.005	52)	04/09/15	0.045 / 0.040	0.041	--
34)	01/02/15	0.040 / 0.035	0.035	-0.010	53)	04/16/15	0.045 / 0.040	0.041	--
35)	01/08/15	0.050 / 0.045	0.046	+0.005	54)	04/23/15	0.055 / 0.050	0.051	--
36)	WI 1MTH	/			55)	04/30/15	0.060 / 0.055	0.056	-0.005
37)	1M ROLL	/			56)	05/07/15	0.070 / 0.065	0.066	--
38)	01/15/15	0.020 / 0.010	0.010	-0.005	57)	05/14/15	0.075 / 0.070	0.071	+0.005
39)	01/22/15	0.010 / 0.005	0.005	--	58)	05/21/15	0.075 / 0.070	0.071	-0.005
40)	01/29/15	0.010 / 0.005	0.005	--	59)	05/28/15	0.080 / 0.075	0.076	--
41)	02/05/15	0.010 / 0.005	0.005	--	60)	06/04/15	0.090 / 0.085	0.086	--
42)	02/12/15	0.005 / 0.000	0.000	--	61)	06/11/15	0.100 / 0.095	0.096	-0.010
43)	02/19/15	0.005 / 0.000	0.000	-0.005	62)	WI 6MTH	/		
44)	02/26/15	0.010 / 0.005	0.005	--	63)	6M ROLL	/		
45)	03/05/15	0.010 / 0.005	0.005	--	64)	06/25/15	0.090 / 0.085	0.086	-0.005
46)	03/12/15	0.035 / 0.025	0.025	--	65)	07/23/15	0.120 / 0.115	0.117	-0.010
47)	WI 3MTH	/			66)	08/20/15	0.130 / 0.125	0.127	-0.005
48)	3M ROLL	/			67)	09/17/15	0.130 / 0.125	0.127	-0.010
49)	03/19/15	0.025 / 0.020	0.020	--	68)	10/15/15	0.140 / 0.135	0.137	-0.005

Australia 61 2 9277 8600 Brazil 5511 2395 9000 Europe 44 20 7330 7500 Germany 49 69 9204 1210 Hong Kong 852 2977 6000
Japan 81 3 3201 8900 Singapore 65 6212 1000 U.S. 1 212 318 2000 Copyright 2014 Bloomberg Finance L.P.
SN 842817 EST GMT-5:00 H435-5570-0 10-Dec-2014 13:03:01

Bloomberg T-bill quotes

Previous slide contains columns with maturity, bid/ask (quoted on discount basis), previous close, and change.

Lets compute some prices from the discounts:

The 6/11/15 maturity has 182 days till expiration from when the quotes were taken on Dec 10, 2014. Thus, the best bid of 0.10 gives a price

$$P_{\text{bid}} = 100 * (1 - 0.001 * 182/360) \approx 99.949444$$

while the best ask of 9.5 BP gives

$$P_{\text{ask}} = 100 * (1 - 0.00095 * 182/360) \approx 99.9519$$

Note that the ask exceeds the bid on a price basis, but the ask is lower than the bid on a discount basis.

Notice that the price of a T-bill can be found from the discount in MS Excel using the function "TBILLPRICE." You can also use the Excel function DAYS() to compute the number of days between the settlement date and the maturity.

So

$$=DAYS('6/11/2015',today()+1)$$

yields 182, and

$$=TBILLPRICE(today()+1,'6/11/2015', 0.0001)$$

gives 99.949444 in Excel.

Bond and note quotes

Bonds are quoted on a *flat price* basis in units of 100. Fractions of a dollar are quoted in units of 32nds. So for example, $100 - 07^14$ means $100 + 7.25/32 = 100.226563$.

The *invoice price* is what the investor actually pays is given by

$$\text{Invoice price} = \text{flat price} + \text{accrued interest} \quad (2)$$

The accrued interest is the interest that the bond has earned since the last coupon payment.

The *flat price* is also called the *clean price*.

The *invoice price* is also called the *dirty price* or *full price*.

<HELP> for explanation.

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U.S. TREASURY 5-10YR NOTES

Page 1/ 1

				<	>	16:48
1)	2 ¹ / ₂	313	96-17+ / 96-18	3.287	+2	
2)	3 ¹ / ₈	413	99-06+ / 99-07	3.301	+2	
3)	3 ¹ / ₂	513	100-25+ / 100-26	3.319	+2 ³ / ₄	
4)	3 ⁵ / ₈	513	101-16 ³ / ₄ / 101-17 ¹ / ₄	3.280	+3 ¹ / ₄	
5)	3 ³ / ₈	513	100-07 ¹ / ₄ / 100-07 ³ / ₄	3.322	+3 ³ / ₄	
6)	4 ¹ / ₄	513	104-13 / 104-13+	3.304	+3 ¹ / ₂	
7)	12	513	101-07 ³ / ₄ / 101-09	1.547	. ³ / ₄	
8)	4 ¹ / ₄	N13	104-15 ¹ / ₄ / 104-15 ³ / ₄	3.329	+3 ³ / ₄	
9)	4	214	103-08 / 103-08+	3.357	+3 ¹ / ₂	
10)	13 ¹ / ₄	514	110-25 ³ / ₄ / 110-28	0.719	+1-20+	
11)	4 ³ / ₄	514	107-09 ¹ / ₄ / 107-10 ³ / ₄	3.362	+2 ¹ / ₂	
12)	12 ¹ / ₂	514	110-17 ³ / ₄ / 112-19 ³ / ₄	1.162	+1-17	
13)	4 ¹ / ₄	514	104-18+ / 104-19 ¹ / ₄	3.410	+2 ¹ / ₄	
14)	4 ¹ / ₄	N14	104-15 / 104-16+	3.454	-. ¹ / ₂	
15)	11 ³ / ₄	N14	111-30+ / 112-30	2.129	+21	
16)	4	215	102-28 / 102-30 ¹ / ₄	3.497	+1 ¹ / ₄	
17)	11 ¹ / ₄	215	144-26+ / 144-27+	3.581	+2 ¹ / ₄	
18)	4 ¹ / ₈	515	103-15 ¹ / ₄ / 103-16	3.546	+1	
19)	4 ¹ / ₄	515	104-02 / 104-02+	3.595	+1 ¹ / ₄	
20)	10 ⁵ / ₈	515	143-05+ / 143-08	3.669	+2 ³ / ₄	
21)	4 ¹ / ₂	N15	105-14 / 105-15+	3.644	+1	
22)	9 ⁷ / ₈	N15	139-11+ / 139-14 ¹ / ₄	3.709	+4 ¹ / ₄	
23)	4 ¹ / ₂	216	105-09 / 105-10 ³ / ₄	3.690	+1 ¹ / ₄	
24)	9 ¹ / ₄	216	136-07 ³ / ₄ / 136-13+	3.718	+7 ¹ / ₂	
25)	5 ¹ / ₈	516	109-05 ¹ / ₄ / 109-05 ³ / ₄	3.766	..	
26)	7 ¹ / ₄	516	122-31 ¹ / ₄ / 123-01 ³ / ₄	3.829	+3	
27)	4 ⁷ / ₈	516	107-09 ¹ / ₄ / 107-09 ³ / ₄	3.820	. ¹ / ₂	
28)	4 ⁵ / ₈	N16	105-16 ¹ / ₄ / 105-16 ³ / ₄	3.846	-2	
29)	7 ¹ / ₂	N16	125-02 / 125-03+	3.948	+2 ¹ / ₄	
30)	4 ⁵ / ₈	217	105-11 / 105-13	3.881	+ ³ / ₄	
31)	4 ¹ / ₂	517	104-09 / 104-09 ³ / ₄	3.920	+1	
32)	8 ³ / ₄	517	134-28+ / 134-29 ¹ / ₄	4.029	+ ³ / ₄	
33)	8 ⁷ / ₈	517	136-10 ¹ / ₄ / 136-11 ³ / ₄	4.064	+1 ¹ / ₄	
34)	4 ³ / ₄	517	106-01 ³ / ₄ / 106-02 ¹ / ₄	3.951	+1	
35)	4 ¹ / ₄	N17	102-08 / 102-08+	3.958	+1	
36)	3 ¹ / ₂	218	96-11 ¹ / ₄ / 96-11 ³ / ₄	3.957	+ ³ / ₄	
37)	3 ⁷ / ₈	518	99-08+ / 99-09	3.963	+1	
38)	9 ¹ / ₈	518	140-16 / 140-18 ³ / ₄	4.087	+2 ³ / ₄	

T/ACT BILLS T/0-1 T/1-2 T/2-5 T/E-10 T/10-20 T/20-30 TIPS STRIPS AG/OTR AGENCIES CURVES
 Australia 61 2 9777 8600 Brazil 5511 3048 4500 Europe 44 20 7330 7500 Germany 49 69 9204 1210 Hong Kong 852 2977 6000
 Japan 81 3 3201 8900 Singapore 65 6212 1000 U.S. 1 212 318 2000 Copyright 2008 Bloomberg Finance L.P.
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The “+” symbol means one half 32d. For example, the bond labelled 3¹8 413 (a 3.125% coupon bond with maturity April 15th, 2013) has a best bid quoted at 99-06+ which equals $99 + 6.5/32 = 99.203125$.

Example

Take for example a bond denoted 4¹/₄ 813.

This note has 4+1/4% coupon and matures Aug 2013. It pays coupon Feb 15th and Aug 15th.

On June 30th, 2008, there were 46 days until the next coupon payment for this bond (31 in July + 15 in August). There were therefore $180 - 46 = 134$ days since the last coupon (Feb 15th).

The accrued interest is therefore

$(4 + 1/4) * (1/2) * (134/180) = 1.581944$. The invoice price is therefore

$$104 + 13/32 + 1.581944 = 105.9882$$

if you buy this bond at the market bid. The invoice asking price is

$$100 + 13.5/32 + 1.581944 = 106.0038$$



Figure : The relationship between retail price and quoted (flat) price. The flat price is below the retail price.

<HELP> for explanation.

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U.S. TREASURY 10-20YR NOTES/BONDS Page 1/ 1

" d " = delayed																											
1)	9 N18	140-09 ³ / ₄	/ 140-11	4.168	+1 ₄																						
2)	8 ⁷ / ₈ 219	139-18	/ 139-19 ¹ / ₄	4.212	+1 ₂																						
3)	8 ¹ / ₈ 819	133-25+	/ 133-26+	4.272	+1																						
4)	8 ¹ / ₂ 220	138-01	/ 138-02 ³ / ₄	4.301	+1 ₄																						
5)	8 ³ / ₄ 520	140-25 ³ / ₄	/ 140-27 ¹ / ₄	4.315	+1 ₂																						
6)	8 ³ / ₄ 820	141-03 ³ / ₄	/ 141-05 ³ / ₄	4.344	-1 ₄																						
7)	7 ⁷ / ₈ 221	133-16	/ 133-17+	4.385	+1 ₄																						
8)	8 ¹ / ₈ 521	136-13	/ 136-14	4.389	-1 ₂																						
9)	8 ¹ / ₈ 821	136-25 ¹ / ₄	/ 136-26 ¹ / ₄	4.401	-1 ³ / ₄																						
10)	8 N21	135-26+	/ 135-27+	4.419	- ³ / ₄																						
11)	7 ¹ / ₄ 822	129-01 ¹ / ₄	/ 129-03	4.452	+1 ₄																						
12)	7 ⁵ / ₈ N22	133-10+	/ 133-12+	4.454	- ³ / ₄																						
13)	7 ¹ / ₈ 223	128-06+	/ 128-07+	4.473	-1																						
14)	6 ¹ / ₄ 823	119-03+	/ 119-05 ¹ / ₄	4.490	-1 ¹ / ₄																						
15)	7 ¹ / ₂ N24	134-23 ¹ / ₄	/ 134-24 ¹ / ₄	4.481	-2																						
16)	7 ⁵ / ₈ 225	136-11 ³ / ₄	/ 136-13 ¹ / ₄	4.492	-2 ¹ / ₄																						
17)	6 ⁷ / ₈ 825	127-21 ¹ / ₄	/ 127-22 ¹ / ₄	4.532	-1 ¹ / ₄																						
						Curve Trades																					
18)	2YR vs 10YR	134.88	/ -135.67																								
19)	5YR vs 10YR	63.81	/ -64.34																								
20)	10Y vs 30YR	54.95	/ -55.34																								
						Other Markets																					
21)	TII 10YR	106-09+	/ 106-11+	0.915	+3																						
22)	TII 30YR	125-25+	/ 125-27+	2.003	-7																						
23)	US Long(CBT)	16:38 d	115-26		+5																						
24)	10Y Fut(CBT)	16:39 d	114-01+		+7																						
25)	5Yr Fut(CBT)	16:39 d	110-19 ³ / ₄		+5 ³ / ₄																						
26)	Fed Funds	16:38	2.500		+1.250																						
27)	EURO\$ (IMM)	16:35 d	97.075		-0.010																						
28)	DowJones Ind	16:30	11350.010		+3.500																						
29)	S&P 500 Ind	16:49	1280.000		+1.620																						
30)	NASDAQ Cmp	16:48	2292.980		-22.650																						
31)	Japanese Yen	16:48	106.182		+0.042																						
32)	EUR-USD	16:49	1.575		-0.004																						
33)	Nymex wti ord	16:19 d	140.550		+0.340																						
T/ACT		BILLS		T/0-1		T/1-2		T/2-5		T/5-10		T/10-20		T/20-30		TIPS		STRIPS		AG/OTR		AGENCIES		CURVES			
Australia 61 2 9777 8600		Brazil 5511 3048 4500		Europe 44 20 7330 7500		Germany 49 69 9204 1210		Hong Kong 852 2977 6000		Japan 81 3 3201 8900		Singapore 65 6212 1000		U.S. 1 212 318 2000													

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- www.treasurydirect.com. The treasury's own wholesale department.
- ftp.publicdebt.treas.gov/dfi/price/ This site gives daily updates of bids/asks for US treasury Bills, notes and bonds. The file "dfi_price_today.txt" contains prices collected at noon.
- www.federalreserve.gov/pubs/feds/2006/200628/feds200628.xls
This is a spreadsheet with historical yield curve data. These are interpolated zero coupon and forward rates. We will use this data later in class.
- www.bgcantor.com. Data products from Cantor.
- Bloomberg terminal in library.

Some useful Excel functions

- `tbillprice(settlement,maturity,discount)` computes the price of a tbill from the discount. It automatically computes a the number of days to expiration based on a 360 day calendar year.
- `coupdaysnc(settlement,maturity,frequency,basis)`. Computes the number of days between "settlement" and the next coupon date. Frequency is the number of coupons/ year (typically 2) and basis is the number of day per year convention (use 0).
- `coupncd(settlement,maturity,frequency,basis)`. Returns the date (as integer) for the next coupon.
- `coupnum(settlement,maturity,frequency,basis)`. Number of coupon payments before expiration.